

Genome rhetoric and the emergence of compositional bias

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Genomes exhibit diverse patterns of species-specific GC content, GC and AT skews, codon bias, and mutation bias. Despite intensive investigations and the rapid accumulation of sequence data, the causes of these a priori different genome biases have not been agreed on and seem multifactorial and idiosyncratic. We show that these biases can arise generically from an instability of the coevolutionary dynamics between genome composition and resource allocation for translation, transcription, and replication. Thus, we offer a unifying framework for understanding and analyzing different genome biases. We develop a test of multistability of nucleotide composition of completely sequenced genomes and reveal a bistability for *Borrelia burgdorferi*, a genome with pronounced replication-related biases. These results indicate that evolution generates rhetoric, it improves the efficiency of the genome's communication with the cell without modifying the message, and this leads to bias.

skew | GC content | codon bias | multistability | coevolution

Living organisms exhibit a variety of statistical patterns of their genome composition (1), including species-specific codon usage bias (2, 3), GC content (4, 5), and asymmetry of nucleotide composition of leading and lagging strands (skews) (6). Despite many proposals, no single satisfactory explanation of skews and their diversity exists (7). Bacterial codon usage also seems complicated and multifactorial; there is evidence for translational selection resulting from uneven expression of the tRNAs (8, 9), optimization of tRNA pools to the existing codon usage (10, 11), and evidence for the primary role of neutral mutational pressure rather than selection (12, 13). Importantly, these mechanisms by themselves do not explain diversity. For example, if codon usage bias is a result of different tRNA pools or mutation pressure in different organisms, why are the tRNA pools or mutation pressure different in the first place?

We propose that a unified account of skews, GC content, and codon usage bias arises from multistability, which, we show, is inherent in the evolution of template-directed synthesis. Instead of treating the mechanisms described above as conflicting alternatives or trying to evaluate their relative importance, we model their coevolution: what happens when tRNAs adjust to codon usage and codon usage adjusts to the tRNAs; what is the outcome when the GC content and skews affect the pool of free nucleotides, and they in turn affect the nucleotide composition and mutation bias? As we will see, the answers to these questions help us integrate the accumulated knowledge about biases and, in addition, suggest bioinformatic tools for examining real genome data, demonstrating multistability and deducing the parameters governing the evolution of biases. As an example, we have determined that multistability of skews and GC content is consistent with the genome sequence of *Borrelia burgdorferi*.

Fig. 1A shows schematically the conventional mutation–selection–drift framework (14), in which selection and mutation pressure are treated as static external variables governing the relaxation of the genome composition to a single state over evolutionary time. Our work describes how the mutation–selection–drift framework can be coupled to the notion of

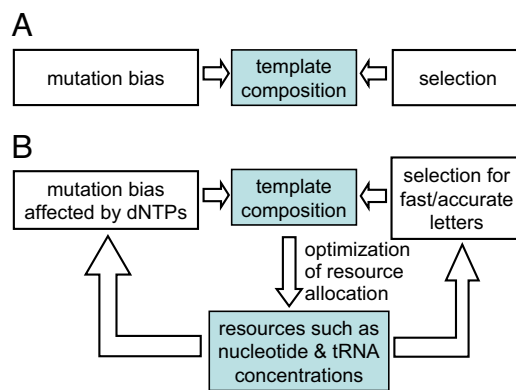


Fig. 1. Contrasting frameworks for studying genome biases. (A) Mutation–selection–drift framework. Selection and mutation pressure are treated as static external variables, and for given values of these inputs the genome composition relaxes to a single state. The variety of genome biases must arise from exogenous mutation and selection pressures. (B) Coevolutionary framework of template-directed synthesis. Resource allocation is introduced as a dynamic degree of freedom. It is optimized to increase the speed, accuracy, and/or energy efficiency for a given template composition and in turn controls the mutation and selection pressures affecting template composition. The feedback loops lead to multistability and diversity of genome biases.

optimal resource allocation for processes of template-directed synthesis within cells (Fig. 1B). The feedback loops that are necessarily involved in such an extension generically lead to multistability (i.e., lack of uniqueness in the possible genome compositions that can arise over evolutionary time) and, as we show, generate a natural explanation of genome biases and their diversity. This framework opens the possibility of reconstructing patterns of genome bias diversity based on universal characteristics of information processing.

The notion of template-directed synthesis captures the common aspects of the central information processes of replication, transcription, and translation (Fig. 2A). During synthesis, a polymerase (DNA or RNA polymerase, ribosome) moves along a template and translates it to a product sequence by discriminating between competing adaptors (tRNAs for translation, dNTPs for replication, NTPs for transcription). The optimal allocation of different adaptors depends on template letter usage, as suggested for translation (10, 11, 15, 16), whereas selection and mutation pressure on letter usage depend on resource allocation (8, 9, 16).

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whether there are genomes that are multistable with their present-day molecular components and mutation rates.

Multistability of GC Content and Skews of Actual Genomes. Ascertaining the possible multistability of actual genomes caused by selection on efficiency of replication is complicated by the lack of experimental data on mutation biases and the coevolution between replication and translation generated biases, which is not modeled here. We try to finesse these difficulties by considering a genome with a dominant replication-related bias and self-consistently deducing the mutation matrix from the known sequence, together with estimates of other model parameters. Specifically, we ask whether there is multistability of skews and GC content arising from the interplay between nucleotide concentrations and nucleotide composition at third codon positions while keeping the rest of the genome, the amino acid composition, and translational selection fixed. Further details are provided in *Materials and Methods*. This is a conservative test of multistability because the amino acid and tRNA usage are artificially kept adjusted to the existing skew and GC content and act to destabilize a state with an alternative 3rd-codon position skew.

We chose to analyze the main chromosome of *B. burgdorferi*, whose nucleotide usage at 3rd-codon positions is mostly determined by the strand, not the codon usage bias (Fig. S1). This is an indication that nucleotide composition is dominated by selection on replication or mutation and allows us to approximately treat translational selection pressures as static. It is possible that the dominance of replication is related to the large number of plasmids in this organism. In addition, the GC and AT skews have stable magnitudes along the chromosome and switch sign sharply near the origin and terminus. Thus, mutation and selection pressures appear independent of position along the chromosome.

We used the condition for optimality of the nucleotide concentrations and the total genome usage of the 4 nucleotides to determine the selection coefficients associated with replication as a function of the ratio κ of DNA elongation and total generation times (see *Materials and Methods*). Combining this with the approximation that translational selection is strand-independent and requiring mutation–selection equilibrium among synonymous groups of 3rd-codon positions on the same strand, we found the synonymous translation selection coefficients R_{sj} and the mutation matrix via a least-square procedure. Overall, the only free parameters in our procedure are κ and the relative nucleotide asymmetries α .

We ran the stochastic coevolutionary dynamics many times and recorded the nucleotide composition of the reached stable states. Strikingly, we found that the simulations predict the existence of an additional stable state with skews of opposite sign and higher GC content (see Fig. 6). This behavior was observed for symmetric nucleotide costs and variations around it. We concluded that the existing data predict evolutionary bistability of the nucleotide composition of *B. burgdorferi* coming from selection on the speed of replication.

This bioinformatic procedure illustrates the possibility of integrating actual genome data with the coevolutionary framework. Other biological constraints can be incorporated.

Dynamic Mutation Model. Many mutations are replication errors and thus affected by the nucleotide concentrations, as indeed has been observed experimentally (24). In this way, mutation turns into a dynamic degree of freedom, as indicated in the *Left* feedback loop of Fig. 1B. Different stable states have not only different adaptor concentrations and genome compositions but also different mutation biases. This finding has important implications for population dynamics. Perhaps paradoxically, even though mutation bias diversity is a consequence of selection on

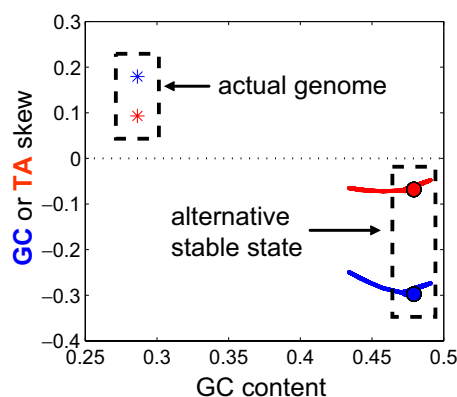


Fig. 6. Predicted bistability of the genome composition of *B. burgdorferi* caused by selection on the speed of replication. The actual genome has GC and TA skews indicated by blue and red stars. Simulations reveal an additional stable state with skews of opposite sign and higher GC content. The location of the second stable state (but not its existence) depends on the free parameter $\kappa \in [0, 1]$ (see *Materials and Methods*). Blue and red balls correspond to $\kappa = 0.5$; blue and red lines correspond to $\kappa \in [0.001, 0.99]$.

the efficiency of template-directed synthesis in this framework, the very fact that letter usage bias is partly channeled through mutational bias would make it difficult to detect the presence of selection at the redundant sites, as shown in Fig. S2. This helps to explain why certain types of statistical analysis appear to show dominance of mutation over selection (12).

Translational Coevolution. Translation is by far the most complex instance of template-directed synthesis. We expect a rich set of patterns emerging from the coevolution of tRNA pools and codon usage, and even tRNA species and codon usage. Although in this article we have presented a model using selection on speed, selection on accuracy can be at least as important and may be naturally incorporated by turning the R_{sj} s into dynamic variables dependent on the tRNA concentrations. The extension to translation would have to account for the fact that tRNAs are often coregulated as parts of operons and in fact might shed a new light on the diversity of the tRNA operon groupings among different organisms.

In addition to its implications for understanding contemporary patterns of codon usage and tRNA pools, the coevolution has implications for early life, when optimization of adaptor pools for speed and accuracy must have been even more important than in the present era because of the lack of compensatory mechanisms such as proofreading. Such models are relevant for understanding the evolvability of the genetic code and its evolution toward optimality (25).

Materials and Methods

Model Details. A quasispecies is assigned a fitness

$$f(c, u) = \frac{G\left(\sum_a \alpha_a c_a\right)}{\Theta + \sum_{si} L_s u_{si}/c_i} \prod_{si} (R_{sj})^{L_{st_{si}}}. \quad [1]$$

Here, G is a decreasing function expressing the cost of production or maintenance of the adaptors. The denominator is the synthesis time T , and its functional form is justified below. (Θ is a constant.) Site-specific selection pressures on letter usage and functional redundancies can be specified by the constants $R_{sj} \in [0, 1]$; they are important in connecting the model to actual genome data. u is normalized so that $\sum_i u_{si} = 1$, L_s is the number of sites of type s , and $L = \sum_s L_s$ is the total genome length. Above, we restricted ourselves to

one-to-one correspondence between adaptors and letters so that c_i is the cognate adaptor to letter i .

The exact interpretation of the denominator of Eq. 1 depends on detailed assumptions, but the functional form is rather generic. In the case of genome replication, we can imagine that cells accumulate resources for time Θ and then replicate for a time that is the sum of the waiting times at each template letter. Θ can also account for the replication time of the functionally conserved sites. Translation and transcription are parallel processes; the synthesis occurs at many sites simultaneously. However, because the elongation speed controls the fraction of busy polymerases and synthesis initiation rate is proportional to the concentration of free polymerases, we end up with the same functional form as in replication (14), but Θ expresses the fraction of polymerases that are idle. The sum in the denominator of Eq. 1 could be weighted to incorporate different gene expression levels, but we do not discuss this extension here.

Dynamics. To relax the letter usage at fixed adaptor concentration, we evolve an infinite asexual population, i.e., $N_e \mu \gg 1$, until it reaches mutation-selection equilibrium. Specifically, let $\{g\}$ be the space of possible genotypes. The abundance n_g of a genotype g with fitness f_g changes because of mutation and selection according to

$$n_g(t+1) = \sum_{g'} \bar{M}_{gg'} f_{g'} n_{g'}(t) \bar{f}_g, \quad [2]$$

where \bar{f} is the mean fitness of the population, and \bar{M} is obtained from M assuming independent point mutations. The next step in the dynamics is the optimization of adaptor concentrations at fixed letter usage. A heritable change in the adaptor pool $\{c\}$ takes over the population with adaptor pool $\{c\}$ if $f(c'; u) > f(c; u)$. This step is not deterministic; different optimizations might be possible. In the simulations we performed, each optimization is followed by a relaxation and each relaxation by an optimization. However, the average equilibrium properties will not depend on the relative rates of relaxation and optimization.

The model above can be directly applied to two-stranded DNA replication in the biologically relevant regime where the lagging strand is limiting the replication speed. However, in some regimes, it is possible to obtain solutions for which the lagging strand is no longer (solely) limiting (see *S1 Text*).

Extracting Site Type Data from Genomes. We determine the origin and terminus of replication from the GC skew and separate the protein-coding regions encoded on the leading and lagging strands. Each 3rd-codon position is assigned to a site type depending on the amino acid it encodes and the strand on which it is encoded. We compute the letter usage u_{si} at each site type s , specifying the frequency i of different synonymous nucleotides. For each strand, we end up with eight 4-fold degenerate site types, 12 2-fold degenerate ones and a 3-fold degenerate one (Ile) (6-fold degenerate amino acids are split into a 4-fold degenerate and a 2-fold degenerate site type). In addition, we record the total nucleotide usage vector (as read from the leading strand) of intergene regions U^{inter} , combined first and second positions U^{12} , and the total nucleotide usage U^{tot} . Fixed 3rd-codon positions coming from Trp and Met, stop codons, overlapping gene portions are added to U^{12} and later treated as nonevolving sites.

Deriving Model Parameters from Genome Data. Letters in the genome experience selection on efficiency of replication, specified by a vector of relative fitness values S_i , and site-specific selection R_{si} coming from functional constraints and selection on efficiency of translation and transcription. At muta-

tion-selection equilibrium, the letter usage vector u_s at 3rd-codon positions of a given site type s is given by

$$\text{Mdiag}(S_a, S_c, S_g, S_t) \text{diag}(R_{sa}, R_{sc}, R_{sg}, R_{st}) u_s = \lambda_s u_s, \quad [3]$$

or in more condensed form (MS) $R_s u_s = \lambda_s u_s$. The site type-independent part $MS \equiv I + E$ is close to the identity matrix because the probability of a letter mutating is very small ($< 10^{-9}$) and the selection on efficiency of replication weak (S_i can be normalized to be close to unity). Correspondingly, $(MS)^{-1} \approx I - E$ within an accuracy far greater than that coming from other assumptions and the mutation-selection equilibrium can be rewritten as

$$r_{si} \equiv \log(R_{si}) = \log \lambda_s - (Eu_s)_i / u_{si}. \quad [4]$$

This choice of R_s (up to an arbitrary multiplicative constant) ensures not only that u_s is an eigenvector of the positive matrix MSR_s , but also, because of the Perron-Frobenius theorem, that it is the unique positive eigenvector corresponding to the largest eigenvalue.

$r_{si} - r_{sj}$ specifies the relative selection coefficients of the letters i and j at a site of type s apart from selection on efficiency of replication. Therefore, for a pair of site types s and s' that have the same functional constraints but are on different strands, we have $r_{si} - r_{sj} = r_{s'i} - r_{s'j}$ for all i and j , and \bar{i} is the Watson-Crick complement of letter i . Here, to have the same MS operating on all site types, the letter usage is read from the same strand. Thus, for a pair of equivalent site types we have

$$(Eu_s)_j / u_{sj} - (Eu_s)_i / u_{si} = (Eu_{s'})_j / u_{s'j} - (Eu_{s'})_i / u_{s'i}. \quad [5]$$

Putting together the equations for all site type pairs and all i and j , we end up with a homogeneous, linear in the elements of E system of equations. Because $\sum_i M_{ij} = 1$, we have the additional nonhomogeneous constraint $\sum_i E_{ij} = S_j - 1 \equiv s_j$. Given S_i and the letter usage u_{si} of enough pairs of functionally distinct site types, we end up with an overdetermined linear system for E . (Although site types differ by 3 numbers, the nonlinear way in which they enter the equations provides linear independence.) By using an exponential $G()$, the condition for adaptor pool optimality $\partial_{c_i} f(c, u) = 0$ gives $U_i^{tot} c_i^{-2} \alpha_i^{-1} = T$. Combining this with $T = \Theta + \sum_i U_i^{tot} c_i^{-1}$ and $s_j = -c_j^{-1} / T$, we obtain

$$s_i = -\kappa \sqrt{\alpha_i / U_i^{tot}} \left(\sum_j \sqrt{\alpha_j U_j^{tot}} \right)^{-1}, \text{ where } \kappa \equiv 1 - \Theta / T. \quad [6]$$

To determine E , we minimize the sum of residuals of system 5 subject to the constraint that the actual genome is a stable steady state of the coevolutionary dynamics. To do so approximately, we solve a quadratic programming problem (minimizing the sum of the residuals of system 5) requiring that all off-diagonal elements of E are greater than ε . We look for the minimum ε (corresponding to least constraint and therefore the smallest residuals) that leads to E for which the observed genome composition is a stable state. For a given matrix E , we find R_{si} from Eq. 4; U^{12} s are assigned to four evolutionary fixed sites types; U^{inter} are lumped into an effective site type with R obtained from Eq. 4. We ran the coevolutionary dynamics many times until an equilibrium was reached and determined whether (i) the actual genome is a stable state or not, and (ii) the system is multistable or not. (We used initial condition $c_i = 10$ for all simulations.) The results presented in Fig. 6 are for $\alpha_i = 1$.

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Supporting Information

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SI Text

Analytic Solution of the Model. Restricting ourselves to gradual changes of $\{c\}$, the condition for adaptor pool optimality is $\partial_{c_i} f(c, u) = 0$, which leads to

$$\frac{u_i}{c_i^2 \alpha_i} = \frac{T}{L} (-G'/G), \quad [\text{s1}]$$

generalizing a scaling relationship between letter usage and adaptor concentrations noted for identical α_i (1) and tested in *Escherichia coli* (2).

The equilibrium n_{gs} correspond to the eigenvector with largest eigenvalue of the matrix $\bar{M}_{gg} f'_g$ (3). In the large-genome limit, the synthesis rate can be expressed as a product of independent fitness contributions for the different sites

$$\frac{1}{T} \infty \prod_s \prod_i \{e^{-c_i^{-1/T}}\}^{L_{s,tsi}} \equiv \prod_s \prod_i F_i^{L_{s,tsi}}, \quad [\text{s2}]$$

and the letter usage relaxation problem reduces to finding the eigenvector u_{si} corresponding to the largest eigenvalue of the matrix $W_{ij}^{(s)} = M_{ij} F_j(T) R_{sj}$ for each site type s , self-consistently with T .

We now solve the one site type, two synonymous letter case $T = \Theta + L(u_1/c_1 + u_2/c_2)$, $R_{11} = R_{12} = 1$. We derive the adaptor bias, $\psi_c = c_2/c_1$ as a function of $\mu \equiv M_{21}$, L , Θ , the mutational bias $m = (M_{21} - M_{12})/M_{21}$, and the adaptor cost bias $\alpha = \alpha_2/\alpha_1$. The letter usage bias is then simply $\psi_u \equiv u_2/u_1 = \alpha \psi_c^2$.

Combining the optimality condition with $u_1 + u_2 = 1$, and assuming $G = \exp(-\sum \alpha_i c_i)$ for algebraic convenience, we obtain

$$F(\psi_c) = \frac{1 - \psi_c}{2\psi_c \theta_1} (1 + \alpha \psi_c) \left\{ \sqrt{1 + \frac{4(1 + \alpha \psi_c^2) \theta_1}{(1 + \alpha \psi_c)^2}} - 1 \right\}. \quad [\text{s3}]$$

where $F(\psi_c) \equiv -L \ln F_2/F_1$ and $\theta_1 = \Theta/(L\alpha_1)$. F_2/F_1 is the relative fitness of the two letters. For $\Theta = 0$, the result is the $\theta_1 \rightarrow 0$ limit of the above but is valid for any decreasing G . (The expression for $F(\psi_c)$ is also valid for two-letter models with many site types.)

Finding the eigenvalues in the limit $\mu \rightarrow 0$, $L \rightarrow \infty$ and solving for μL , we obtain

$$\mu L = F(\psi_c) \frac{\alpha \psi_c^2}{1 + \alpha \psi_c^2} \frac{1}{1 + \alpha \psi_c^2 (m - 1)}. \quad [\text{s4}]$$

Combining Eq. s4 and Eq. s3, we get the equilibrium solutions $\mu L(\psi_c)$ for any Θ , α , and m . For values of μL for which we have three ψ_c , the middle solution is always unstable, as shown by the red line on Fig. 5. The maximum μL for which bistability is possible (the transition point) is determined from $d(\mu L)/d\psi_c = 0$ as a function of m and α .

For $\Theta = 0$, $\alpha = 1$, $m = 0$ the expression simplifies to $\mu L = \psi_c/(1 + \psi_c)^2$. The symmetric solution $\psi_c = 1$ is stable above the transition point $\mu L = 1/4$ (Fig. 5, blue line). For extreme mutational bias, $m \rightarrow 1$, and $\Theta = 0$, the transition point approaches from above $(\mu L)_{min}^* = (2 + \alpha - 2\sqrt{1 + \alpha})/\alpha$. Thus, for $\alpha = 1$, it shifts only from 1/4 to $3 - 2\sqrt{2} \approx 0.17$.

Consistency Condition for the Two-Stranded Model. Selection on the replication speed for the two-stranded DNA model can be modeled with

$$T = \Theta_0 + \max \left(\Delta_{LAG} + \sum_i \frac{U_i}{c_i}, \sum_i \frac{U_i}{c_{\bar{i}}} \right), \quad [\text{s5}]$$

where $\Delta_{LAG} > 0$ is the additional waiting time for lagging strand replication (coming from primer synthesis, etc.), U_i is the usage on the lagging strand, and \bar{i} is the Watson-Crick complement of a letter i . This model reduces to the generic single-template model with $\Theta = \Theta_0 + \Delta_{LAG}$ if the following consistency condition is satisfied

$$\Theta > \Delta_{LAG} > \sum_i U_i \left(\frac{1}{c_{\bar{i}}} - \frac{1}{c_i} \right).$$

Dynamic Mutation Model. Let $M_{ji}^{(0)}$ be the probability that nucleotide j is accepted, once it has arrived at the active site of the polymerase, given a template letter i . Then, the mutation rate coming from replication is

$$M_{ji} = M_{ji}^{(0)} c_j / \sum_k M_{ki}^{(0)} c_k. \quad [\text{s6}]$$

The matrix $M^{(0)}$ is a molecular property of the replication machinery, whereas M is an observable property of the cell.

The equilibrium behavior of this model as a function of $M^{(0)}$ is generally very similar to that of the static model as a function of M , except for the neutral and symmetric case $M_{ji}^{(0)} = (1 - \epsilon)\delta_{ij} + \epsilon(1 - \delta_{ij})$. In this regime, the solution is equivalent to that of the static model, if we replace μL with $\epsilon^2 L$, leading to \sqrt{L} scaling, rather than independence of L , of the transition point expressed as mutations per genome per generation. This scaling disappears in the presence of asymmetries or nonneutral sites, but the transition is typically shifted to the right, extending the region of bistability, as shown by the black curves in Fig. S2.

A statistical signature of selection is the deviation of $D \equiv (M_{21}u_1)/(M_{12}u_2)$ from unity, the value expected for purely mutational equilibrium. We plot this quantity for the static and dynamic mutational models in the symmetric case, and in the presence of 1% fixed sites (half of them belonging to 1, and the other half to 2). Whereas in the static model the statistical signature of selection rises sharply immediately below the transition (Fig. S2, solid red), in the dynamic model it stays close to unity well into the symmetry broken phase (Fig. S2, dashed red).

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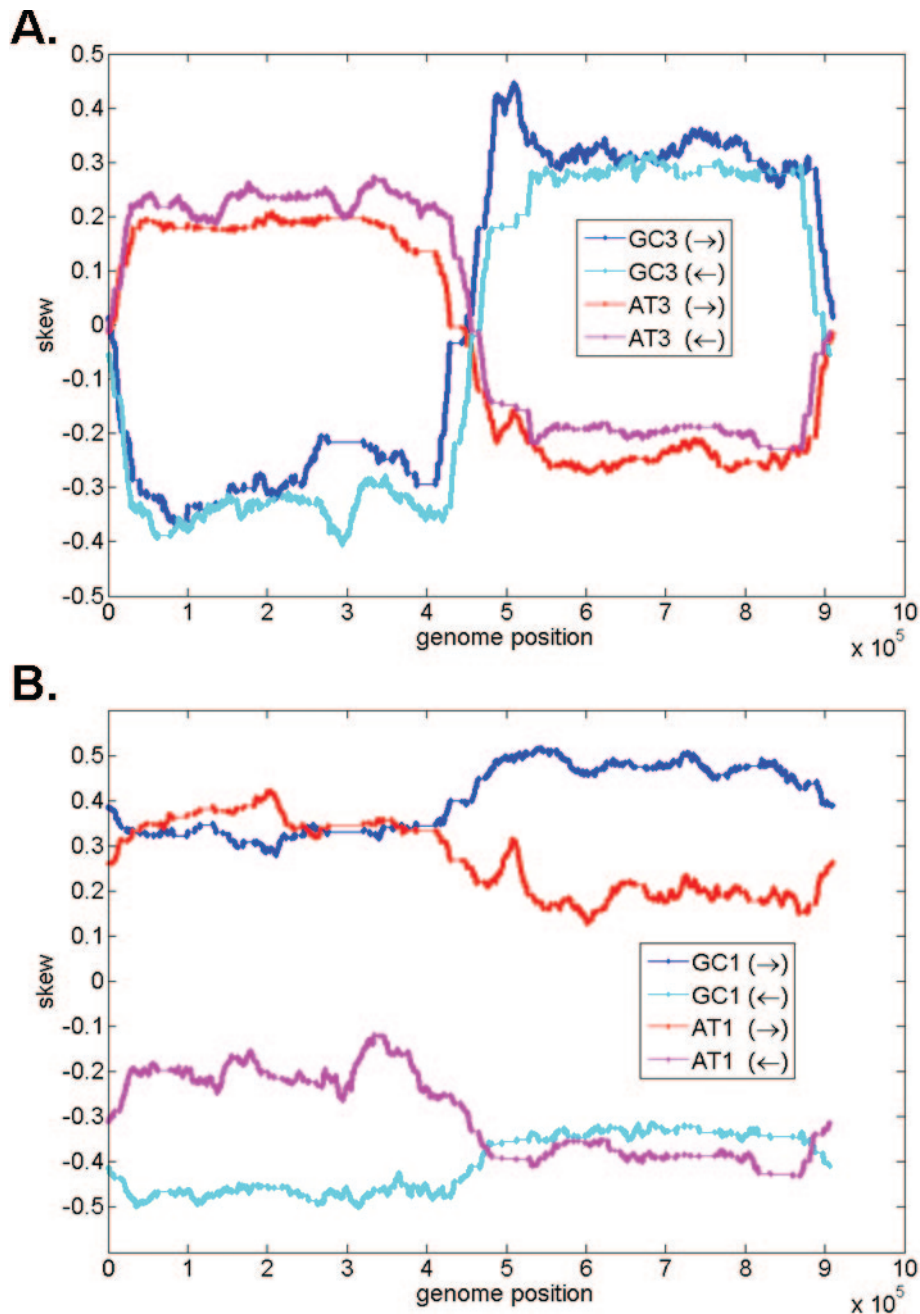


Fig. S1. Third- and first-codon position skews of *Borrelia burgdorferi* obtained by sliding a 10-kb window. To separate replication-related bias from codon usage and gene orientation bias, we compare the nucleotide skews of genes encoded to the left with those encoded to the right. (A) Third-codon position skews are almost the same for the two gene orientations (blue curve is close to light blue curve, and red curve is close to magenta curve), indicating that strand rather than codon bias is the primary factor shaping nucleotide usage at 3rd-codon positions. Skews switch sign at the origin of replication located near the middle of the linear chromosome. (B) First-codon position skew curves are offset vertically for the two gene orientations, indicating that functional constraints (e.g., typical amino acid usage) contribute significantly to nucleotide usage. Strand bias has a contribution as well, as seen from the steps in the curves near the middle of the genomes.

